6.002 - Lecture 11

Inductors

- Inductors are Everywhere
- Uses
- Basic Physics
- First-Order ODEs









www.GEGridSolutions.com



Wiring Inductance



$$L \approx \mu_{o} R \left[ln \left(\frac{16 R}{D} \right)^{-2} \right]$$



$$L = \frac{\mu_0}{\pi} \ln \left[\frac{S}{R} + \sqrt{\left(\frac{S}{R}\right)^2 - 1} \right]$$
Per Length

<u>Uses</u>

Inductor Uses:

- Energy Storage
- Energy Transduction (Transformers)
- Position and Motion Sensing
- Actuation (Motors)
- Generation (Generators)
- Memory (Original Core Memory!)
- Frequency-Domain Filtering
- Time-Domain Dynamics
- Resonators
- Timing

Ideal Inductor



Two signs Possible Stored Energy Reversible

Common Nonidealities

- Winding series resistance
- Core loss and saturation
- Winding capacitance

A lumped-parameter model can often represent these non ideal behaviors.



Dynamics & Memory



- Flux linkage (and current) depends on the entire voltage history.
- * Flux linkage summarizes (memorizes) the voltage history relevant to the future.

State Continuity



- Lim T \rightarrow 0 : $\lambda(t) \rightarrow$ step and v(t) $\rightarrow \infty$
- Without infinite voltage, λ(t) cannot step and so is continuous

Power & Energy





Inductor Combinations



 $+\mathcal{V}_1 - +\mathcal{V}_2 -$

$$\frac{di}{dt} = \frac{di_1}{dt} + \frac{di_2}{dt}$$
$$= \frac{l}{L_1} \mathcal{V} + \frac{l}{L_2} \mathcal{V}$$
$$= \left(\frac{l}{L_1} + \frac{l}{L_2}\right) \mathcal{V}$$

Effective reciprocal inductance ⇒ reciprocal parallel inductances add

Series

╊

'n

$$V = V_1 + V_2$$

= $L_1 \frac{di}{dt} + L_2 \frac{di}{dt}$
= $(L_1 + L_2) \frac{di}{dt}$

Effective inductance >> Series inductances add

RL Node Analysis



Exponential Decay

