6.002 - Lecture 13

Pulses, Impulses & More

- Various Inputs
- Pulse Input
- Impulse Input
- Linearity
- Superposition
- Initial Conditions

<u>Useful Inputs</u>



Exponential-Related Inputs

Sin(wt) Cos (wt)

Sinh (1/2) Cosh (t/z)

Frequency Response

Step & Impulse



Step ult) and impulse Sits occur when their arguments are zero.

Current & Voltage Impulses



Step Response Review



 $RC \frac{dV_c(t)}{dt} + V_c(t) = Ri_{(N}(t), V_c(-\infty) = 0$



Current Pulse Response





Current Impulse Response I



All charge goes into the capacitor over the duration of the Employ.

Current Impulse Response II

Physical Observations:

- No source current passes through the resistor. If any fraction of the current impulse passed through the resistor, then the voltage across the resistor, and hence across the capacitor in parallel with it, would be an impulse. To drive an impulse of capacitor voltage requires a doublet of source current which is not specified. Therefore, the current impulse passes entirely through the capacitor delivering its charge Q to the capacitor. The capacitor voltage then steps to Q/C by t = 0⁺.
- After t = 0⁺, the impulse source current is zero and the capacitor voltage decays exponentially according to the homogeneous response of the network.

Current Impulse Response II



Zero input \Rightarrow homogeneous response for t>0 \Rightarrow V(t) = V(ot) e^{-t/RC}. What is V(ot)?

$$Rc \frac{d v(t)}{dt} + v(t) = RQ \delta(t)$$

$$Rc \int_{0}^{0} \frac{d v(t)}{dt} dt + \int_{0}^{0} v(t) dt = RQ \int_{0}^{0} \delta(t) dt$$

$$Rc \left[v(t) - v(t) \right] + 0 = RQ$$

$$V(t) = v(t) + Q$$

Linearity I

Lineavity > Superposition & Homogeneity r = 0 $i_2(t)$ $T \rightarrow t$ $-\frac{Q}{T}$ $V(t) = \frac{PQ}{T}(1-e^{-t/RC})$ ult First Step: $V(t) = -\frac{FQ}{T}(1 - e^{-rC})u(t-T)$ Second Step: $V(t) = \frac{RQ}{T} \left(1 - e^{-t/PC} \right) \quad 0 \leq t \leq T$ Superposition: $V(t) = \Pr_{+}^{e} \left(1 - e^{-T_{RL}}\right) e^{-\left(\frac{t-T}{RC}\right)} t^{2T}$ i PRICT-

Linearity II



Initial conditions should be treated as independent sources derving superposition.

Linearity III

